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The Assimilation of Satellite Derived Sea Surface Temperatures into a Diurnal Cycle Model

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T Assi i i S i i S Su
T p u si i C

$$\mathbf{x} \mathbf{P}$$
 $\mathbf{x} \mathbf{p}$ $\mathbf{x$

*For y ni ersity of Re ding no t Dep rt ent of E rth ciences i on Fr ser ni ersity B rn y British Co i A C n d s n pi en s scepti e to di rn hr ing sign s hr herefore the ti ing of the o ser tions in the conditions in thic

tion co p risons re di c t nd errors ry for di erent regions nd ti e sc es in di rn cyc e ode ing the high es re not of concern s no di rn sign for s t high ind speeds ho e er the di rn r ing is ery sensiti e to s ight ch nges in ind speeds t the o es he ind speed w is i port nt ec se ind stress incre ses ro gh y s w nd i ed yer deepening ith w herefore e en s ight i ses in N P se s rf ce inds speeds c n e d to syste tic errors in oce n circ tion ode s th t re forced y these inds ind speeds of ess th n s⁻ cco nt for ne ry of g o ho ry er ged inds e inds re concentr ted in the tropics nd C re is t en to con ert the si ho ry integr ted so r fro ECM F to represent the si ho ry integr ted so r fro ECM F to $cyc e^{rA}$ his is chie ed y integr ting the Reed for o er si ho r indo gi ing

$$\int_{T}^{T^{\perp}} I \, dt \quad \int_{T}^{T^{\perp}} I_{\downarrow} \quad - \quad \cdot \quad n_{I} \quad \cdot \quad \beta^{*} \quad -\alpha^{*} \, dt, \qquad \qquad \checkmark^{*}$$

here *I* is the tot s rf ce so r r di tion nd I_{\downarrow} is the s rf ce inso tion nder ce r s ies the fr ction c o d co er e is denoted y *n* edo y α β is the so r noon ng e nd *T* re the si ho ry eteoro ogic n ysis ti es he eft h nd side of Eq tion $\dot{\gamma}$ is set eq to the integr ted ECM F e nd Eq tion $\dot{\gamma}$ c n then e re rr nged to rnd n e ecti e e n c o d p r eter o er this indo

$$n \quad \frac{\beta_T \int_T^{T, \, \smile} I_{\downarrow} - \alpha_T^{\dagger} dt - \int_T^{T, \, \smile} I \, dt}{\int_T^{T, \, \smile} I_{\downarrow} - \alpha_T^{\dagger} dt}.$$

if it is night so that $\int_T^{T-} I_{\downarrow} - \alpha dt$ then persistence $n n_{-}$ denotes e ch hr n ysis ti e is ss ed A chec is so de to enforce the physic c o d i its $\leq n \leq 1$ he net s rf ce R I sed in the ode r n is c c ted t e ery ti e step sing the Reed for ith the si ho r y derived c o d es h s ch ener ti esc e is chie ed hie the si ho r y integr ted ECM F es re ret ined

ho ry

his section descri es ethod for t ning the cod coer nd the s rf ce ind speed pr eters s they pper in the forcing gorith s for the GOM ode it is ss ed th t these top r eters re i e y to e the ost poor y non fron NP or re n ysis ode o tp t the pr eters re sed to hep GOM it i e s te ite e s re ents inc ding the di rn cyce co ponent

3.1 The Algorithm

 $\begin{array}{c} \text{if } \stackrel{\bullet}{} e \quad \text{consider the ode ed} \quad \stackrel{\bullet}{} \theta \quad \text{s f nction of the fr ction } c \ o \ d \ co \ er \ n \\ nd \quad \text{ind speed forcing } \stackrel{\theta}{w} \quad \sqrt{u} \quad v \end{array}$

$$heta \quad heta \quad n,w^{\dagger}.$$

P r _eters ϵ_A nd ϵ_B re introd ced here

$$n \quad n \quad \epsilon_A,$$

$$w \qquad , \quad \epsilon_B^{\dagger} w , \qquad \delta^{\dagger}$$

$$\int \epsilon B^{\frac{1}{2}} \sqrt{u} \int v$$

hese d st ent pr eters i e ss ed to re in r ed o er e ch ho r ti e indo j tho gh the c gro nd d t u v nd n fro ECM F ch nge e ery si ho rs he c o d correction is seen to e n so te error here s the ind correction is fr ction error his oids corrections to ind direction nd o s the strict i its on c o d co er $\leq n \leq$ to e s tis ed he c n no e ie ed s f nction of the p r eters

$$\theta \quad \theta \quad \epsilon_A, \epsilon_B^{\dagger}$$
 .

e no de cost f nction $J = J \epsilon_A, \epsilon_B$ s

$$J = \sum_{s} \left(H \; \theta^{\text{modely}} - \theta^{\circ s} \right),$$

A here N is the n r of o ser tions o er the hor r indo r d t Td t Td t Td

T

 $\epsilon_B > \frac{1}{2}$ he d t ssi i tion pro e c n no est ted s fo o s An `optimal' parameter pair $\epsilon_A^*, \epsilon_B^{**}$ is sought such that for all feasible $\epsilon_A, \epsilon_B^{**}$

$$|J \ \epsilon_A^*, \epsilon_{B'}^{*}| \le |J \ \epsilon_A, \epsilon_{B'}^{*}|.$$

 \mathfrak{f} t is possi e th t n incre se in c o d co er nd decre se in \mathfrak{f} ind speeds nd ice ers co d pro ide the desired e ect \mathfrak{f} n this scen rio

o ser tions fro AMRE nd M¢ if oth types iR nd M 7 of o ser tions re i e then on y the ind pr eter is t ned t if on y M o ser tions re i e then oth ind nd c o d p r eters re t ned to nderesti te the r ing on these occ sions of e er e rier in the ee the ode ed di $\overset{\text{H}}{\text{m}}$ r ing esti tes re rger than the oser tions s ggest he d't ssi i tion ethod red ces the cod if necess ry in the presence of E (R) o ser tions fooded y correction to the ind speed forcing and then the cod fr ctions hen E (R) oser tions re not present he ssi i tion is e to red ce the ode ed r ing for d ys through to and increase the di random random on d ys and the soft the oser tions choose cose y On d ys and the ssi i tion hence cess the syste does not f y dhere to the ssi ptions of the ssi i tion ro time either ec se the esti ted sensiti ity o er the properties range is in cc r te or the req ired change in forcing is o tside the st ted restrictions



d y O (A sho's 'r i s co p red to the o ser tions nd this is i e y the c se of the ssi i tion r n to f i t this point he ssi i tion is ess ro st if correction to the di rn cyce is sed on sing e o ser tion p rtic r y if it occ rs e r y in the orning his c n e seen in Fig re, here on d y sight correction e r y in the 'r ing ph se e ds to rger di rn cyce th t c n not e ttested y f rther o ser tions nd on d y here s res t of possi e erroneo s y coo o ser tion strong inds re sed to e i in te ny di rn cyce hese e p es i str te ho the sche e co d e f rther i pro ed in the f t re y incorpor ting ore o ser tions nd i ding on the no edge g ined to for c ref tre t ent of o ser tion error oth syste tic nd r ndo i thin the ssi i tion cyce









4.2 Comparing Di erent Satellite Observations

F rther n yses ere so perfor ed to ssess the errors ssoci ted ith indi id o ser tion types re ti e to the contro r n nd these re presented in e

_	No O s	Me n	▶ D	RM
GO M E (R)				
GO M AM RE				
GO M Mí				

e Results showing the number of observations, the mean, STD, and RMS of $\theta_{control} - \theta_{obs}$, in °C, for individual satellite types for the area – °N to – °N and °E to , °E during st { th January 2006.

A si i r n er of E $\{R\}$ nd AM RE o ser tions re i e o er the ti e period in this re ith sight y fe er M $\{$ o ser tions he ode o ser tion tch ps re e di erences et een the three s te ite instreents he E $\{R\}$ o ser tions re sho n to e on er ge r er th n the p r efferised s in te per t re here s the AM RE nd M $\{$ o ser tions re coo er on er ge th n the ode ed his s ggests th t the o ser tions h e so e syste tic errors in this re t this ti e ith E $\{R\}$ syste tic y too r n nd or AM RE nd M $\{$ o ser tions syste tic y too coo he ode co d so h e r is nd e estituting too gre t coo s in correction his see s ni e y s the p r efferised coo s in correction for this period s on er ge r th n the P r efferised st rt of e ch d y therefore ny errors in O $\{A$ i so e pp rent see ection ?he D nd RM re signific nt y o er hen co p ring E $\{R\}$ o ser tions here the RM error ppro ches °C

4.3 Day-Night Comparisons

Di erences in night ti e et een the restricted hors of c ti e nd dyti e et een the hors c ti e the so ere so

	Me n	₱ D	RM
Before Assi i tion			
d yti e			
night fi e			
After Assi i tion			
d yti e			
night tige			

for heighten di rn cyc e nd dr 's the ode coser to the oser tions[†] he [†] D nd RM di erences re in si i r for oth d y nd night

[↑] e. Results showing the mean, STD, and RMS of $\theta_{model} - \theta_{obs}$, before and after the assimilation, in °C, during daytime (10{16}) and night time (22{04}) local time for the area - °N to - °N and, °E to, °E during st{ th January 2006.

4.4 Comparisons to OSTIA

 \bullet o he p deter ine to \bullet h t e tent the i ses

re fo nd to e rger th n night ti e i ses nd hen co p ring o ser tions i s of -. °C is fo nd his indic tes th t the s te ite o ser tions on er ge re r er th n O (A s o d e e pected ec se O (A is rge y restricted to night ti e he sh rp di erence in d y nd night ti e e n es de onstr tes the presence of di rn sign s in the d yti e o ser tions O (A is the en e of these o ser tions s e s others nd so the e pect tion is th t the i s o d e s (n this tch p o ser tions re inc ded here s O (A is for ed y e i in ting d yti e o ser tions t en ith ind speeds ess th n s⁻ hese ddition o ser tions re therefore contri ting to the sight coo i s in

	No O s	Me n	RM	₱ D
ECM F AM RE	÷	†	¢	ţ
A JM AM RE			`	· · · · · · · · · · · · · · · · · · ·
ECM F Mí	4	†	4	¢.
A íM Mí	,	— . _、		
ECM F ALL	+	, †	<i>†</i>	P
ssi ALL		- **		

F

e Results comparing the ECMWF forecast wind speeds before and after assimilation to the AMSRE and TMI wind measurements showing the number of observations, the mean, the RMS, and STD di erences in ms⁻. For the area – °N to – °N and, °E to, °E during st{ th January 2006. The numbers in parenthesis are calculations only at the locations and times when wind speeds are corrected in the assimilation.

(n this p per d t ssi i tion ethod h s een de e oped th t ssi i tes s te ite deri ed o ser tions into di rn cyce ode (t is proposed ho ode errors in di rn r ing esti tes re pri ri y c sed y ncert inties in N^H P forcing d t he di rn ri i ity of s c n e ie ed s f nction of ind speeds nd fr ction c o d co er O ser tions fro E (R) AM RE nd M) occ rring thro gho t the d y re co p red to their ode ed eq i ent he res ting di er ences re then red ced y ing corrections to the forcing ind speeds nd c o d co er his t ning of the forcing is sho n to res t in ode ed esti tes th t rese e i e o ser tions ch ore cose y he ssi i tion ethod co d e ie ed s s oothing nd interporting the s te ite o ser tions in n inte igent nner he ethod is sho n for p to the oser tions etter th n O (A hich ses d i y persistence ss ption Most ssi i tion sche es do not se ertic corre tion sc es hen inserting o ser tions nd s seq ent y re n e to pro ide d st ents to the s s rf ce ther odyn ic str ct re this red ces the e ecti eness of n ssi i tion

Most ssi i tion sche es do not se ertic corre tion sc es 'hen inserting o ser tions nd s seq ent y re n e to pro ide d st ents to the s s rf ce ther odyn ic str ct re this red ces the e ecti eness of n ssi i tion o e er y correcting ind speed nd c o d co er es ithin ncert inty o nds the ethod presented here tte pts to preser e the nce of ther nd dyn ic 'e ds' ithin the di rn ther oc ine

the ethod presented here the pts to preser e the nce of ther nd dyn ic re ds ithin the di rn ther oc ine his ssi i tion ethod co d e i pe ented on ch ider sc e to i d p det i ed re ti e pict re of di rn r ing cross the ords oce ns he distri tion nd gnit de of di rn sign s re sti re ti e y n no n nd this techniq e of erging o ser tions ith di rn cyc e ode co d e sed to i pro e this sit tion Another pp ic tion co d e to se this techniq e to c c te fo n d tion te per t res of incre sed cc r cy For e to to to to the to

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